

# Soustava lineárních rovnic - řešení

$$I. \quad 3x + 5y + z + t = 0$$

$$II. \quad 2x + 3y - z + 2t = 0$$

$$III. \quad x + 2y + z - t = 0$$

$$IV. \quad 4x + 5y - 5z + 8t = 0$$

$$\left( \begin{array}{cccc|c} 3 & 5 & 0 & 1 & 0 \\ 2 & 3 & -1 & 2 & 0 \\ 1 & 2 & 1 & -1 & 0 \\ 4 & 5 & -5 & 8 & 0 \end{array} \right) \sim \left( \begin{array}{cccc|c} -1 & -2 & -1 & 1 & 0 \\ 2 & 3 & -1 & 2 & 0 \\ 3 & 5 & 0 & 1 & 0 \\ 4 & 5 & -5 & 8 & 0 \end{array} \right) \sim \left( \begin{array}{cccc|c} 1 & 2 & 1 & -1 & 0 \\ 0 & -1 & -3 & 4 & 0 \\ 0 & -1 & -3 & 4 & 0 \\ 0 & -3 & -9 & 12 & 0 \end{array} \right) \sim$$

$\cdot 2 = -2, -4, -2, 2 \mid 0$   
 $\cdot 3 = -3, -6, -3, 3 \mid 0$   
 $\cdot 4 = -4, -8, -4, 4 \mid 0$

$$\sim \left( \begin{array}{cccc|c} 1 & 2 & 1 & -1 & 0 \\ 0 & -1 & -3 & 4 & 0 \end{array} \right) \begin{array}{l} I. \\ II. \end{array}$$

Máme 4 neznámé a pouze 2 rovnice  $\Rightarrow$  2 volitelné parametry

$$II. \quad -y - 3z + 4t = 0$$

$$y = 4t - 3z$$

$$\vec{r} = (5z - 7t; 4t - 3z; z; t)$$

$$I. \quad x + 2(4t - 3z) + z - t = 0$$

$$x + 8t - 6z + z - t = 0$$

$$x + 7t - 5z = 0$$

$$x = 5z - 7t$$